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# Crystal structure and lattice dynamics of $\mathrm{Sr}_{3} \mathrm{Y}\left(\mathrm{BO}_{3}\right)_{3}$ 

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#### Abstract

X-ray, Raman and infrared (IR) studies of the $\mathrm{Sr}_{3} \mathrm{Y}\left(\mathrm{BO}_{3}\right)_{3}$ (BOYS) single crystal grown by the Czochralski technique are presented. The crystal structure is trigonal, space group $R \overline{3}$ (no. 148), and comprises six formula units in the unit cell with the hexagonal axes $a=12.527$ (2) and $c=9.280(2) \AA$. The assignment of the observed vibrational modes is proposed on the basis of lattice dynamics calculations. The unusual large bandwidth of the internal modes and the enhancement of the principal mean square thermal displacements for $\mathrm{BO}_{3}$ and $\mathrm{Y}(1)$ indicate that some type of disorder is present in the studied crystal.


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## 1. Introduction

Yb -doped materials, both crystals and glasses, are of great interest due to their potential applications in diode-pumped solidstate lasers. The simple electronic structure of $\mathrm{Yb}^{3+}$ ion eliminates unwanted effects such as excited-state absorption or upconversion. Moreover, small quantum defect limits the losses of the pumping power and the broad emission band allows the generation of femtosecond pulses. Therefore, Yb-doped materials can be used in high-power continuous wave lasers for material processing, as well as in femtosecond sources and tunable lasers in the near infrared (IR) [1]. One of the promising materials for Yb doping is the $\mathrm{Sr}_{3} \mathrm{Y}\left(\mathrm{BO}_{3}\right)_{3}$ (BOYS) crystal [2-7]. It was shown, for instance, that Yb -doped BOYS crystal is a good candidate for femtosecond lasers fabrication: BOYS: Yb (20 at\%) crystal was used in the construction of mode locked laser emitting 69 fs pulses at the central wavelength of 1062 nm [2].

Synthesis of strontium rare-earth borates described by the formula $\mathrm{Sr}_{3} \operatorname{Ln}\left(\mathrm{BO}_{3}\right)_{3}(\mathrm{Ln}=\mathrm{Y}, \mathrm{Pr}-\mathrm{Lu})$ was reported by Khamaganova et al. [5]. BOYS: Yb single crystals were grown using the Czochralski technique [6]. The crystal structure of BOYS was not resolved but it was reported that it is isostructural with $\mathrm{Sr}_{3} \mathrm{Sc}\left(\mathrm{BO}_{3}\right)_{3}$ borate, which crystallizes in the $R \overline{3}$ structure $[6,8]$. The former studies revealed that phonon relaxations play an important role in the emission properties of this borate doped

[^0]with $\mathrm{Er}^{3+}$ and $\mathrm{Yb}^{3+}$ [4]. Moreover, some bands observed in the emission and absorption spectra could be attributed to vibronic features [9,10]. However, phonon properties of this material are not known. Therefore, it is of interest to perform studies of the phonon properties of BOYS in order to understand spectroscopic features of the rare-earth ions in this matrix.

In this paper, results of X-ray diffraction, polarized Raman and IR studies as well as lattice dynamics (LD) calculations of the BOYS single crystal are reported. The experimental data along with the LD calculations give very accurate assignment of the observed modes and information on longitudinal optical (LO)-transverse optical (TO) splitting for this crystal.

## 2. Experimental

Single crystals of BOYS were grown using the Czochralski method. The thermal system consisted of a 53 mm outer diameter, $50-\mathrm{mm}$-high and $1.5-\mathrm{mm}$-thick iridium crucible, in passive iridium afterheater placed around the crucible top on the grog, and alumina heat shields around the afterheater. A charge material was prepared on the base of high purity ( 4.5 N ) oxides and carbonate: $\mathrm{Y}_{2} \mathrm{O}_{3}, \mathrm{~B}_{2} \mathrm{O}_{3}, \mathrm{Yb}_{2} \mathrm{O}_{3}$ and $\mathrm{SrCO}_{3}$. After mixing, the charge material was heated at $1150^{\circ} \mathrm{C}$ for 6 h in a resistivity furnace to obtain the BOYS compound. The growing atmosphere was pure nitrogen. The following conditions of the growth processes were applied: growth rate $0.6-1.2 \mathrm{~mm} \mathrm{~h}^{-1}$; rotation rate $5-20 \mathrm{rpm}$; cooling after growth-at least 24 h . Firstly, single crystals were obtained by spontaneous nucleation on the

Table 1
Crystal data and structure refinement parameters for BOYS

| Formula weight | 386.38 |
| :--- | :--- |
| Temperature $(\mathrm{K})$ | $293(2)$ |
| Wavelength $(\AA)$ | 0.71073 |
| Crystal system, space group | Trigonal, $R \overline{3}$ |
| Unit-cell dimensions ( $\AA$ ) |  |
| $a$ | $12.5270(18)$ |
| $c$ | $9.2800(19)$ |
| $\gamma$ (deg) | 120 |
| Volume ( $\AA^{3}$ ) | $1261.2(4)$ |
| $Z$, calculated density ( $\mathrm{mg} \mathrm{m}^{-3}$ ) | $6,4.173$ |
| Absorption coefficient $\left(\mathrm{mm}^{-1}\right)$ | 25.792 |
| $F$ (000) | 1440 |
| Crystal size (mm) | $0.22 \times 0.18 \times 0.14$ |
| $\Gamma$ Range for data collection | $3.25-47.69$ |
| Limiting indices | $-21 \leqslant h \leqslant 26 ;-16 \leqslant k \leqslant 25 ;-12 \leqslant l \leqslant 19$ |
| Reflections collected/unique | $9676 / 2517\left[R_{\text {int }}=0.082\right]$ |
| Completeness to $\Gamma=47.31$ | $94.44 \%$ |
| Refinement method | Full-matrix least-squares on $F^{2}$ |
| Data/restraints/parameters | $2517 / 0 / 51$ |
| Goodness-of-fit on $F^{2}$ | 1.009 |
| Final $R$ indices $[I>2 \sigma(I)]$ | $R_{1}=0.0485, w R_{2}=0.0865$ |
| Extinction coefficient | 0.0092 |
| Largest diff. peak and hole $\left(\mathrm{e} \AA^{-3}\right)$ | 2.310 and -3.112 |

platinum wire. Then seeds cut off the crystals were used. The obtained single crystals up to 15 mm in diameter and $35-50 \mathrm{~mm}$ in length were free of macroscopic defects and inclusions of other phases. All the single-crystal boules were annealed in oxidizing atmosphere at $950^{\circ} \mathrm{C}$ for 3 h , and then slowly cooled down to room temperature.

The single-crystal sample of dimensions given in Table 1 was selected for X-ray diffraction data collection with a four-circle diffractometer KM-4/CCD (Oxford Diffraction). The instrument was operated in $\kappa$ geometry and used $\mathrm{Mo} K \alpha$ radiation ( $\lambda=0.71073 \AA$ ). The 1150 images were taken in nine runs with different angular settings and applying the $\omega$-scan mode ( $\Delta \omega=1^{\circ}$ for each image, the exposure time was 25 s ). Diffraction data were integrated for intensities and corrected for Lorentzpolarization effects using the CrysAlis program package [11]. The structure was solved by Patterson and electron density syntheses. The calculations were performed with the SHELX-97 program system [12].

Polycrystalline IR spectra were measured from the grounded crystals with a Biorad 575C FT-IR spectrometer in KBr suspension for the $1200-400 \mathrm{~cm}^{-1}$ region and in Nujol suspension for the $500-30 \mathrm{~cm}^{-1}$ region. Polarized IR spectra of a single crystal were measured in the $E \| x$ and $E \| z$ geometries at near normal incidence of $10^{\circ}$ using a specular reflectance accessory. FT-Raman spectra were measured for an oriented single crystal using the BRUKER $110 / \mathrm{S}$ spectrometer with the YAG: $\mathrm{Nd}^{3+}$ excitation. Both IR and Raman spectra were recorded with a spectral resolution of $2 \mathrm{~cm}^{-1}$.

## 3. Results

### 3.1. Structure determination

The BOYS compound is trigonal, space group $R \overline{3}$ (no. 148), and comprises six formula units in the unit cell with the hexagonal axes $a=12.527$ (2) and $c=9.280(2) \AA$. The crystal data, experimental details, and the structure refinement parameters are given in Table 1.

The structural motif consists of the strontium-oxygen polyhedron, two symmetrically distinct $\mathrm{YO}_{6}$ octahedra, and the $\mathrm{BO}_{3}$ triangle (Figs. 1 and 2). The atomic positional parameters are given in Table 2. The compound is isomorphous with $\mathrm{Sr} \mathrm{S}_{3} \mathrm{Sc}\left(\mathrm{BO}_{3}\right)_{3}$ [8],


Fig. 1. View of the crystal structure of BOYS along the $c$-axis.


Fig. 2. View of the crystal structure of BOYS along the $b$-axis.

Table 2
Atomic coordinates $\left(\times 10^{4}\right)$ and equivalent isotropic displacement parameters ( $\AA \times 10^{3}$ ) for BOYS

|  | $X$ | $Y$ | $z$ | $U_{\text {eq }}$ |
| :--- | :--- | :--- | :--- | :--- |
| $Y(1)$ | 0 | 0 | 0 | $19(1)$ |
| $Y(2)$ | 0 | 0 | 5000 | $51(1)$ |
| $\mathrm{Sr}(1)$ | $1205(1)$ | $3718(1)$ | $233(1)$ | $29(1)$ |
| B | $1520(4)$ | $2018(4)$ | $2485(5)$ | $20(1)$ |
| $\mathrm{O}(1)$ | $539(4)$ | $1808(4)$ | $1619(6)$ | $68(1)$ |
| $\mathrm{O}(2)$ | $2658(4)$ | $2487(3)$ | $1982(5)$ | $65(1)$ |
| $\mathrm{O}(3)$ | $1284(5)$ | $1784(4)$ | $3911(4)$ | $72(1)$ |

$U_{\text {eq }}$ is defined as one-third of the trace of the orthogonalized $U_{i j}$ tensor.
but differs in details resulting from different covalent radii, $R$, of the Y and Sc -atoms. In the octahedral coordination, $R_{\mathrm{Sc}}=1.610$ and $R_{Y}=1.780 \AA$ [13]. While in the Sc derivative, the Sr -atom exhibits nine-fold coordination, in the present structure the Sr-atom is an eight-fold coordinate (Table 3). The Y-atoms occupy two symmetrically independent Wyckoff positions $3 a:(0,0,0)$ and

Table 3
Selected bond lengths ( $\AA$ ) and angles (deg)

| $\mathrm{B}-\mathrm{O}(1)$ | $1.380(6)$ |
| :--- | :--- |
| $\mathrm{B}-\mathrm{O}(2)$ | $1.325(6)$ |
| $\mathrm{B}-\mathrm{O}(3)$ | $1.356(6)$ |
| $\mathrm{Sr}(1)-\mathrm{O}(2) \# 1$ | $2.439(4)$ |
| $\mathrm{Sr}(1)-\mathrm{O}(1)$ | $2.666(5)$ |
| $\mathrm{Sr}(1)-\mathrm{O}(2) \# 3$ | $2.524(4)$ |
| $\mathrm{Sr}(1)-\mathrm{O}(1) \# 4$ | $2.647(5)$ |
| $\mathrm{Sr}(1)-\mathrm{O}(3) \# 2$ | $2.680(5)$ |
| $\mathrm{Sr}(1)-\mathrm{O}(2) \# 5$ | $2.724(5)$ |
| $\mathrm{Sr}(1)-\mathrm{O}(3) \# 4$ | $2.894(5)$ |
| $\mathrm{Sr}(1)-\mathrm{O}(3) \# 5$ | $2.902(5)$ |
| $\mathrm{Y}(1)-\mathrm{O}(1)$ | $2.513(4) 6 \times$ |
| $\mathrm{Y}(2)-\mathrm{O}(3)$ | $2.238(4) 6 \times$ |
| $\mathrm{O}(2)-\mathrm{B}-\mathrm{O}(1)$ | $122.5(5)$ |
| $\mathrm{O}(2)-\mathrm{B}-\mathrm{O}(3)$ | $120.6(5)$ |
| $\mathrm{O}(1)-\mathrm{B}-\mathrm{O}(3)$ | $116.7(4)$ |

Symmetry transformations used to generate equivalent atoms: \#1 $-x+1 / 3,-y+2 / 3$, $-z+2 / 3 ; \# 2 y-2 / 3,-x+y-1 / 3,-z+2 / 3 ; \# 3-x+y-1 / 3,-x+1 / 3, z+1 / 3 ; \# 4 x+1 / 3, y+2 / 3$, $z+2 / 3$; \#5 $x-y+1 / 3, x+2 / 3,-z+2 / 3$.

Table 4
Anisotropic displacement parameters $\left(\AA^{2} \times 10^{3}\right)$ for BOYS

|  | $U_{11}$ | $U_{22}$ | $U_{33}$ | $U_{23}$ | $U_{13}$ | $U_{12}$ |
| :--- | ---: | ---: | ---: | :--- | :--- | ---: |
| $\mathrm{Y}(1)$ | $16(1)$ | $16(1)$ | $24(1)$ | 0 | 0 | $8(1)$ |
| $\mathrm{Y}(2)$ | $16(1)$ | $16(1)$ | $119(1)$ | 0 | 0 | $8(1)$ |
| $\mathrm{Sr}(1)$ | $30(1)$ | $26(1)$ | $21(1)$ | $-1(1)$ | $2(1)$ | $8(1)$ |
| B | $28(3)$ | $9(2)$ | $27(3)$ | $6(2)$ | $11(2)$ | $12(2)$ |
| $\mathrm{O}(1)$ | $53(3)$ | $56(3)$ | $109(4)$ | $-35(2)$ | $-43(2)$ | $37(2)$ |
| $\mathrm{O}(2)$ | $42(2)$ | $32(2)$ | $96(3)$ | $-12(2)$ | $39(2)$ | $0(2)$ |
| $\mathrm{O}(3)$ | $126(4)$ | $41(2)$ | $38(2)$ | $8(2)$ | $15(2)$ | $34(3)$ |

The anisotropic displacement factor exponent takes the form $-2 \pi^{2}\left[h^{2} a^{2} U_{11}+\cdots+2\right.$ $\left.h k a b U_{12}\right]$.

3d: $\left(0,0, \frac{1}{2}\right)$, forming an octahedra with quite different configuration. The $\mathrm{Y}(1)-\mathrm{O}_{6}$ distances equal to $2.513(4) \AA$, while the $\mathrm{Y}(2)-\mathrm{O}_{6}$ distances are $2.238(4) \AA$. The $\mathrm{O}-\mathrm{Y}-\mathrm{O}$ angles indicate significant octahedral distortion since in the $\mathrm{Y}(1) \mathrm{O}_{6}$ they range from $87.92(2)^{\circ}$ to $92.1(2)^{\circ}$, yet in $\mathrm{Y}(2) \mathrm{O}_{6}$ the distortion is even larger, as the octahedral angles run from 78.8(1) ${ }^{\circ}$ to $101.2(1)^{\circ}$. The $\mathrm{BO}_{3}$ triangles are not regular (Table 3). The average B-O distance $1.354(5) \AA$ is shorter than in the Sc-containing structure with the corresponding bond equal to $1.38(1) \AA$.

The $\mathrm{YO}_{6}$ octahedra are linked through the borate group into the chain with alternating $\mathrm{Y}(1)$ and $\mathrm{Y}(2)$ polyhedra running along the crystal $c$-axis (Fig. 2). Besides, the octahedron centered about $\mathrm{Y}(1)$ shares all vertices with the Sr -polyhedra, while in the $\mathrm{Y}(2) \mathrm{O}_{6}$ these are the faces common with the Sr-polyhedron. This diversity in linkages explains the elongation of the $\mathrm{Y}(1)-\mathrm{O}$ and shortening of the $\mathrm{Y}(2)-\mathrm{O}$ distances. By sharing corners, edges, and faces the Sr polyhedra form a three-dimensional framework, interconnected via borate groups with the $\mathrm{YO}_{6}$ octahedra.

It is worth adding that some types of disorder (static or dynamic) in the present crystal cannot be excluded, since the principal mean square thermal displacements are enhanced for $\mathrm{BO}_{3}$ and $\mathrm{Y}(1)$ (Table 4).

### 3.2. Raman and IR spectra

For the $R \overline{3}$ structure of BOYS group theory predicts $15 A_{\mathrm{g}}+$ $15 E_{\mathrm{g}}+17 A_{\mathrm{u}}+17 E_{\mathrm{u}}$ Brillouin zone center modes. These modes can be subdivided into $2 A_{\mathrm{g}}+2 E_{\mathrm{g}}+2 A_{\mathrm{u}}+2 E_{\mathrm{u}}$ asymmetric stretching ( $v_{3}$ ), $A_{\mathrm{g}}+E_{\mathrm{g}}+A_{\mathrm{u}}+E_{\mathrm{u}} \quad$ symmetric stretching $\quad\left(v_{1}\right), \quad 2 A_{\mathrm{g}}+2 E_{\mathrm{g}}+2 A_{\mathrm{u}}+2 E_{\mathrm{u}}$


Fig. 3. Polarized Raman spectra (a) as well as polycrystalline IR spectra in the midIR (b) and far-IR (c) regions.
in-plane bending $\left(v_{4}\right), A_{\mathrm{g}}+E_{\mathrm{g}}+A_{\mathrm{u}}+E_{\mathrm{u}}$ out-of-plane bending ( $v_{2}$ ), $3 A_{\mathrm{g}}+3 E_{\mathrm{g}}+3 A_{\mathrm{u}}+3 E_{\mathrm{u}}$ translational and $3 A_{\mathrm{g}}+3 E_{\mathrm{g}}+3 A_{\mathrm{u}}+3 E_{\mathrm{u}}$ librational modes of the $\mathrm{BO}_{3}^{3-}$ groups. The remaining modes correspond to translations of the $\mathrm{Sr}^{2+}\left(3 A_{\mathrm{g}}+3 E_{\mathrm{g}}+3 A_{\mathrm{u}}+3 E_{\mathrm{u}}\right)$ and $\mathrm{Y}^{3+}\left(2 A_{\mathrm{u}}+2 E_{\mathrm{u}}\right)$ ions. It should be remembered, however, that among the translational modes, two modes ( $A_{\mathrm{u}}$ and $E_{\mathrm{u}}$ ) belong to the acoustic branches. The $A_{\mathrm{g}}$ and $E_{\mathrm{g}}$ modes are Raman active, and the $A_{\mathrm{u}}$ and $E_{\mathrm{u}}$ modes are $I R$ active. This analysis shows that one expects to observe 30 modes in Raman and 32 modes in IR spectra.

Room-temperature Raman spectra of the BOYS single crystal measured in different polarization configurations as well as the polycrystalline IR spectra are shown in Fig. 3. Fig. 4(a) presents the polarized IR spectra measured for the single crystal. These polarized IR spectra were fitted by using four parameters model in order to give information about TO and LO wavenumbers [14]. According to this model, the complex dielectric constant is expressed in terms of the IR-active modes as follows:
$\varepsilon(\omega)=\varepsilon_{\infty} \prod_{j} \frac{\omega_{j \mathrm{LO}}^{2}-\omega^{2}+\mathrm{i} \omega \gamma_{j \mathrm{LO}}}{\omega_{j \mathrm{TO}}^{2}-\omega^{2}+\mathrm{i} \omega \gamma_{\mathrm{jTO}}}$
where $\omega_{j \text { TO }}$ and $\omega_{j \text { LO }}$ correspond to the resonance wavenumbers of the $j$ th transversal and longitudinal modes, respectively, and $\gamma_{j \text { TO }}$ and $\gamma_{j \mathrm{LO}}$ are the corresponding damping factors. $\varepsilon_{\infty}$ is the dielectric constant. For normal incidence, the IR reflectivity $R$ and the dielectric function are related by
$R=\left|\frac{\sqrt{\varepsilon}-1}{\sqrt{\varepsilon}+1}\right|^{2}$
The results of fitting of the experimental data to the fourparameter model are summarized in Table 5, where oscillator strengths $\Delta \varepsilon_{\mathrm{TO}}$ are also given. The plots of the calculated wavenumber dependence of the absorption coefficient and


Fig. 4. Polarized reflection spectra (a), absorption coefficient (b) and imaginary part of the inverse dielectric function (c) for the BOYS crystal.

Table 5
Dispersion parameters for the best fit to the reflectivity data of BOYS for $E \| x$ and E\||z polarization

| $\omega_{\text {TO }}\left(\mathrm{cm}^{-1}\right)$ | $\gamma_{\text {TO }}\left(\mathrm{cm}^{-1}\right)$ | $\omega_{\mathrm{LO}}\left(\mathrm{cm}^{-1}\right)$ | $\gamma_{\mathrm{LO}}\left(\mathrm{cm}^{-1}\right)$ | $\Delta \varepsilon_{\text {TO }}$ |
| :--- | :---: | :---: | :---: | :--- |
| $E \\| x$ |  |  |  |  |
| 257.0 | 40.7 | 257.3 | 47.9 | 0.009 |
| 372.5 | 60.1 | 392.9 | 54.4 | 0.51 |
| 568.8 | 91.8 | 569.0 | 65.3 | 0.006 |
| 575.7 | 64.9 | 586.7 | 106.7 | 0.175 |
| 749.5 | 20.1 | 766.2 | 15.9 | 0.251 |
| 791.8 | 14.7 | 793.2 | 14.2 | 0.014 |
| 1178.8 | 96.0 | 1193.7 | 134.5 | 0.076 |
| 1279.3 | 67.6 | 1331.3 | 78.4 | 0.156 |
|  |  | $\varepsilon_{\infty}=2.89$ |  |  |
|  |  |  |  |  |
| $E \\| z$ |  |  |  |  |
| 373.6 | 57.0 | 401.6 | 39.7 | 0.127 |
| 577.8 | 38.1 | 580.4 | 41.6 | 0.023 |
| 740.5 | 31.6 | 740.7 | 34.8 | 0.002 |
| 756.0 | 115.3 | 757.2 | 101.5 | 0.014 |
| 1177.2 | 84.8 | 1245.3 | 75.7 | 0.500 |
| 1270.6 | 81.9 | 1357.1 | 100.7 | 0.089 |
|  |  | $\varepsilon_{\infty}=2.86$ |  |  |

imaginary part of the inverse dielectric function are presented in Figs. 4(b) and (c), respectively. The maxima of these plots correspond to TO and LO wavenumbers. Inspection of Table 5 shows that the largest LO-TO splittings, up to $86.5 \mathrm{~cm}^{-1}$, are observed for the $v_{3}$ modes.

Table 6
Potential parameters used for the lattice dynamics calculations

| $i$ Th ion | $z_{i}(\mathrm{e})$ | $a_{i}(\AA)$ | $b_{i}(\AA)$ | $C\left(\mathrm{kcal}^{1 / 2} \AA^{3} \mathrm{~mol}^{1 / 2}\right)$ |
| :--- | :---: | :--- | :--- | :--- |
| Sr | 1.2 | 1.575 | 0.08 | 0 |
| Y | 1.35 | 1.378 | 0.09 | 0 |
| B | 1.5 | 0.429 | 0.08 | 0 |
| O | -1.05 | 1.841 | 0.16 | 20 |
| Ion pair | $D_{j i}\left(\mathrm{kcal} \mathrm{mol}^{-1}\right)$ | $\beta_{i j}(\AA)$ | $r_{i j}{ }^{*}(\AA)$ |  |
| B-O | 26.0 | 2.72 | 1.44 |  |

### 3.3. LD calculations

In order to adequately assign the Raman peaks to the atomic vibrations, we performed LD calculations. Since BOYS is mostly ionic, we performed the calculations on the basis of a partially ionic model described in the paper by Nozaki et al. [15]. The atomic positions used in the calculations were taken from the above-discussed X-ray structural studies. The following interatomic potential was used in the LD calculations:

$$
\begin{align*}
U_{i j}\left(r_{i j}\right)= & \frac{z_{i} z_{j} e^{2}}{r_{i j}}+\left(b_{i}+b_{j}\right) \exp \left[\frac{a_{i}+a_{j}-r_{i j}}{b_{i}+b_{j}}\right]-\frac{c_{i} c_{j}}{r_{i j}^{6}} \\
& +D_{i j}\left(\exp \left[-2 \beta_{i j}\left(r_{i j}-r_{i j}^{*}\right)\right]-2 \exp \left[-2 \beta_{i j}\left(r_{i j}-r_{i j}^{*}\right)\right]\right) \tag{3}
\end{align*}
$$

This interatomic potential consists of a Coulomb interaction (first term) to model the long-range interactions; a Born-Mayertype repulsive interaction (second term) for accounting the shortrange forces; a van der Waals attractive interaction (third term) to model the dipole-dipole interaction and finally the Morse potential contribution (last term) for taking into account the covalent bond character. $z_{i}$ and $z_{j}$ are the effective charges of the ions $i$ and $j$, respectively, separated by the distance $r_{i j}$. The parameters $\left(a_{i}, a_{j}\right)$ and $\left(b_{i}, b_{j}\right)$ correspond to the ionic radii and ionic stiffness, respectively. The initial values of the parameters for the oxygen and boron were taken from Ref. [16]. The initial values of $z$ and $b$ parameters for $\mathrm{Sr}^{2+}$ and $\mathrm{Y}^{3+}$ were the same as those used for $\mathrm{Ca}^{2+}$ and $\mathrm{Gd}^{3+}$ in the LD calculations for $\mathrm{Ca}_{4} \mathrm{GdO}\left(\mathrm{BO}_{3}\right)_{3}$ [16]. Since the parameters $a$ reflect the radii, they were obtained for the $\mathrm{Sr}^{2+}$ and $\mathrm{Y}^{3+}$ ions using the values for the $\mathrm{Ca}^{2+}$ and $\mathrm{Gd}^{3+}$ reported in Ref. [16] and the expressions $a_{\mathrm{Sr}}=a_{\mathrm{Ca}} r_{\mathrm{Sr}} / r_{\mathrm{Ca}}$ and $a_{\mathrm{Y}}=a_{\mathrm{Gd}} r_{\mathrm{Y}} / r_{\mathrm{Gd}}$. The initial parameters were changed during the calculations in small steps in order to obtain the best agreement between the observed and calculated wavenumbers. The final parameters used in the present calculations are listed in Table 6. Since we consider covalency for the B-O bond only, $D_{i j}, \beta_{i j}$ and $r_{i j}{ }^{*}$ are given for this bond. The calculated and experimental frequencies are shown in Table 7. The standard error of estimate of the calculated and experimental vibrational modes is $36.8 \mathrm{~cm}^{-1}$.

## 4. Discussion

The former studies of borates showed that the internal modes of the planar $\mathrm{BO}_{3}^{3-}$ ion are observed around 900-1060 (( $v_{1}$ ), $650-800\left(v_{2}\right), 1200-1500\left(v_{3}\right)$ and $540-680 \mathrm{~cm}^{-1}\left(v_{4}\right)$, respectively [16-19]. The present study is in agreement with the results obtained for other borates, showing that the wavenumbers of fundamental vibrations of the $\mathrm{BO}_{3}^{3-}$ ions are grouped into four distinct regions, i.e., 1323-1177, 943-926, 796-749 and $623-569 \mathrm{~cm}^{-1}$. The polarization behavior of the Raman bands is not clearly observed, but our LD calculations help in assigning the modes to the respective symmetries, as proposed in Table 7. It is worth noting that in the $796-749 \mathrm{~cm}^{-1}$ region, three Raman bands

Table 7
Experimental and calculated vibrational modes of BOYS and their assignment

| Raman |  |  |  |  | IR |  |  |  |  | Assignment |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & z(x x) z \\ & A_{\mathrm{g}}+E_{\mathrm{g}} \\ & \text { Obs. } \end{aligned}$ | $\begin{aligned} & y(z z) y \\ & A_{\mathbf{g}} \\ & \text { Calc. } \end{aligned}$ | Obs. | $\begin{aligned} & y(x z) y \\ & E_{\mathrm{g}} \\ & \text { Calc. } \end{aligned}$ | Obs. | Polycrystalline Obs. | $E \\| x$ <br> $E_{\mathrm{u}}$ <br> Calc. | Obs. | $\begin{aligned} & E \\| z \\ & A_{\mathrm{u}} \\ & \text { Calc. } \end{aligned}$ | Obs. |  |
|  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
| 1298 | 1306 | 1323 | 1300 | 1281 | 1281 | 1295 | 1279 | 1307 | 1271 | $\nu_{3}\left(\mathrm{BO}_{3}\right)$ |
| 1189 | 1139 | 1191 | 1102 | 1184 | 1194 | 1133 | 1179 | 1104 | 1177 | $\nu_{3}\left(\mathrm{BO}_{3}\right)$ |
| 942+928 | 956 | 943 | 948 | 942+928 | 926 | 956 |  | 934 |  | $v_{1}\left(\mathrm{BO}_{3}\right)$ |
| 796 |  |  |  |  | 793 |  |  |  |  | $v_{2}\left(\mathrm{BO}_{3}\right)$ |
| 772+749 | 789 |  | 745 |  | 752 | 667 | 749 | 718 | 756 | $v_{2}\left(\mathrm{BO}_{3}\right)$ |
| 610 | 636 | 623 | 639 | 607 | 609 | 652 | 576 | 625 |  | $v_{4}\left(\mathrm{BO}_{3}\right)$ |
| 594 | 600 | 598 | 612 | 598 | 581 | 613 | 569 | 587 | 578 | $v_{4}\left(\mathrm{BO}_{3}\right)$ |
|  | 415 |  | 412 |  |  | 416 |  | 417 |  | $T^{\prime \prime}\left(\mathrm{BO}_{3}\right)$ |
| 363 | 402 |  | 380 | 370 |  | 395 | 372 | 385 | 373 | $\mathrm{L}\left(\mathrm{BO}_{3}\right)$ |
| 319 | 347 | 357 | 322 | 315 | 327 | 324 |  | 345 |  |  |
| 279 | 272 |  | 281 | 270 |  | 284 |  | 321 |  |  |
|  | 252 | 224 | 255 |  | 246 | 256 | 257 | 258 |  |  |
| 186 | 185 | 185 | 225 | 181 | 208 | 192 |  | 209 |  | $T^{\prime}\left(\mathrm{Sr}^{2+}\right)$ |
|  | 125 |  | 153 | 142 |  | 181 |  | 163 |  |  |
| 120 | 111 | 119 | 122 |  |  | 143 |  | 127 |  |  |
|  | 73 |  | 98 |  |  |  |  |  |  |  |
|  |  |  |  |  |  | 107 |  | 116 |  | $T^{\prime}\left(\mathrm{Y}^{3+}\right)$ |
|  |  |  |  |  |  | 85 |  | 77 |  |  |

are observed although only two are predicted by the group theory ( $A_{\mathrm{g}}+E_{\mathrm{g}}$ ). Possibly, the extra band arises due to the Fermi resonance between the $v_{2}$ modes and an overtone of a lattice mode. We cannot, however, exclude the possibility that the extra Raman band arises from the $749 \mathrm{~cm}^{-1}$ IR-active band, which becomes weakly active in the Raman scattering due to some disorder. It is worth to note that one additional band in this wavenumber region was observed by us previously also for $\mathrm{Ca}_{4} \mathrm{GdO}\left(\mathrm{BO}_{3}\right)_{3}$ [16]. Another characteristic feature of the IR and Raman bands in the internal modes region is their large bandwidth. Former optical studies of BOYS doped with $\mathrm{Yb}^{3+}$ ions also showed that this borate exhibits a particularly broad zero-phonon absorption line, which enables efficient diode pumping of the crystal at 980 nm and tuning of the laser emission over a very large wavelength range ( $1020-1090 \mathrm{~nm}$ ) [1,6]. This feature was assigned to the presence of two distinct sites occupied by $\mathrm{Y}^{3+}$ ions [9]. The presence of two $\mathrm{Y}^{3+}$ sites cannot, however, explain the observed large bandwidth for the internal modes of the $\mathrm{BO}_{3}^{3-}$ ions because these ions occupy only one site. Our results give, therefore, a strong argument that some type of disorder is present in the studied crystal. The Raman data support, therefore, the conclusion derived from the X-ray studies that some type of disorder in this crystal might be present.

Let us now discuss the origin of the bands observed below $400 \mathrm{~cm}^{-1}$. These bands correspond to librational and translational motions of the $\mathrm{BO}_{3}^{3-}$ units, and translational motions of the $\mathrm{Sr}^{2+}$ and $\mathrm{Y}^{3+}$ ions. Factor group analysis predicts that there should be 18 Raman- and 20 IR-active modes in this region. It is worth adding that translational modes of the $\mathrm{Y}^{3+}$ ions are not active in the Raman spectra. Inspection of the spectra shows that the number of observed modes is much smaller than predicted. This result indicates that many modes have similar wavenumbers and are therefore not resolved in the room-temperature spectra. The former studies showed that translational modes of $\mathrm{Ca}^{2+}$ ions are observed in the $300-120 \mathrm{~cm}^{-1}$ region [16]. Since the atomic mass of $\mathrm{Sr}^{2+}$ ions is significantly larger than that of $\mathrm{Ca}^{2+}$, the corresponding modes should be observed at lower wavenumbers. Our LD calculations indicate that the largest contribution of the translational motions of $\mathrm{Sr}^{2+}$ ions should be observed for the modes observed in the $208-142 \mathrm{~cm}^{-1}$ region. In a similar way, we may expect to observe the translational modes of the $\mathrm{Y}^{3+}$ ions at higher wavenumbers than the corresponding modes of the $\mathrm{Gd}^{3+}$
ions. The comparison of the spectra with the results obtained for $\mathrm{Ca}_{4} \mathrm{GdO}\left(\mathrm{BO}_{3}\right)_{3}$ and $\mathrm{NdFe}_{3}\left(\mathrm{BO}_{3}\right)_{4}$, for which translations of $\mathrm{Gd}^{3+}$ and $\mathrm{Nd}^{3+}$ were located below $120 \mathrm{~cm}^{-1}[16,20]$ shows that these modes should be observed below $160 \mathrm{~cm}^{-1}$. Our LD calculations are in agreement with this assumption since they show the largest contribution from translational motions of the $\mathrm{Y}^{3+}$ ions is expected for the two lowest wavenumber IR modes (see Table 7). However, the corresponding IR bands are probably very weak and cannot be clearly seen due to overlapping with much stronger and very broad bands observed at higher wavenumbers. The remaining bands below $400 \mathrm{~cm}^{-1}$ can be assigned to the lattice vibrations of the $\mathrm{BO}_{3}^{3-}$ ions. These modes are strongly coupled but our LD calculations suggest that the higher wavenumber modes have larger contribution of the translational motions and the lower wavenumber modes have larger contribution of the librational motions.

## 5. Conclusions

X -ray structural studies revealed that the Y -atoms, substituting Sc in $\mathrm{Sr}_{3} \mathrm{Sc}\left(\mathrm{BO}_{3}\right)_{3}$ compound, caused distinct shifts of the $\mathrm{BO}_{3}$ groups located in the general Wyckoff positions (18f). Consequently, in the BOYS structure, the oxygen sublattice becomes substantially distorted and the polyhedral distortions are significantly larger than in the Sc derivative.

The performed Raman and IR studies and the performed LD calculations allowed us to establish symmetries of the observed vibrational modes and propose assignment of the observed modes to the respective vibrations of structural units. They also confirmed the conclusion obtained from the crystallographic studies that some type of disorder (static or dynamic) is present in this crystal.

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